

# Focusing of internal waves

Experimental study

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Réunion du GdR Turbulence  
Grenoble, LEGI 1/06/2015



# Contents

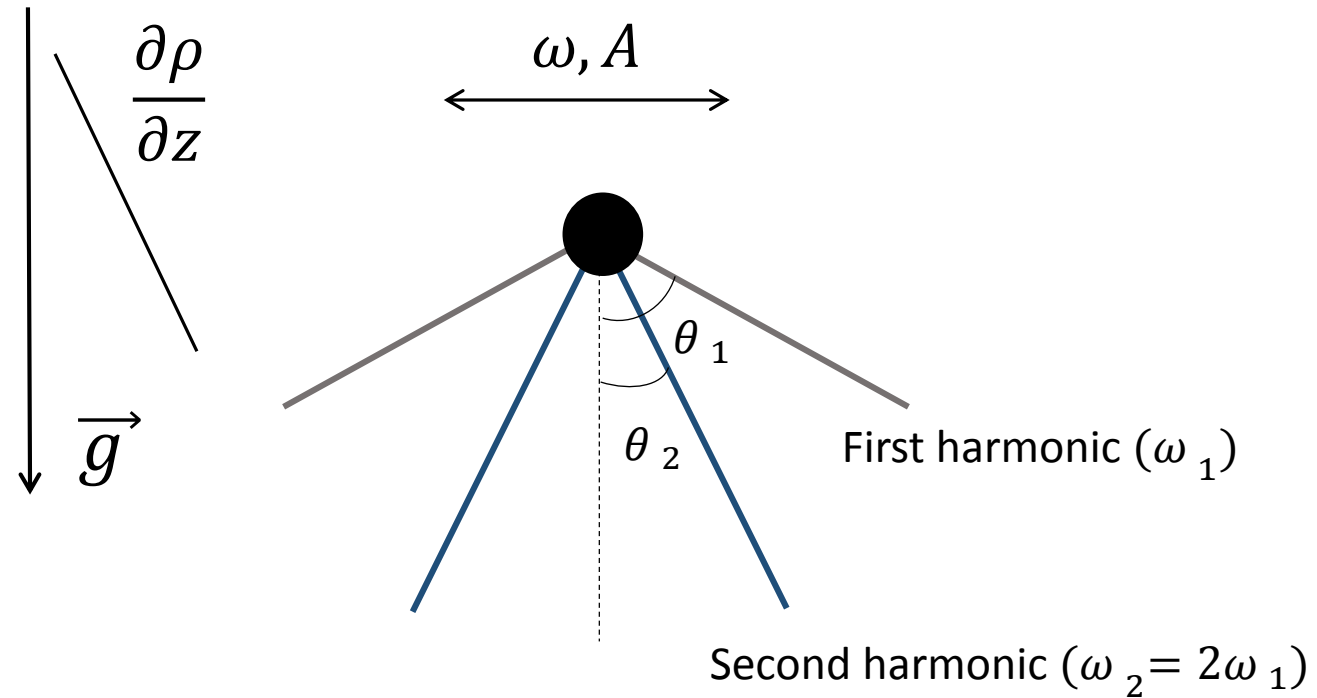
- Comparison of experimental results with linear theory (first order waves)
- Secondary waves (higher harmonics)
- Increase of oscillation amplitude  $\rightarrow$  nonlinear regime

# Internal gravity waves

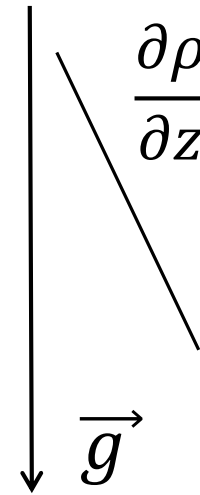
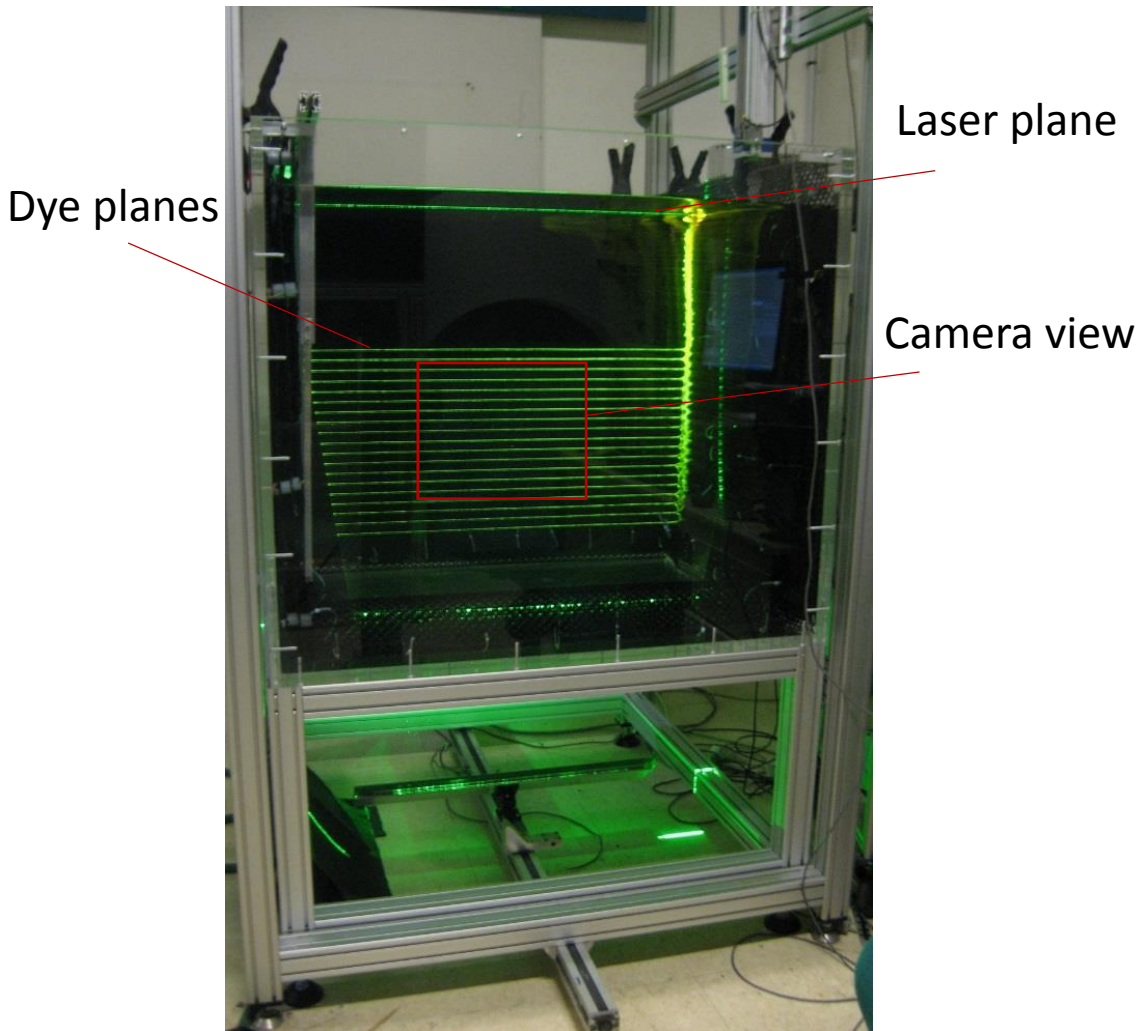
Buoyancy frequency:  $N = \left[ \left( -\frac{g}{\rho} \right) \left( \frac{\partial \rho}{\partial z} \right) \right]^{1/2}$

Dispersion relation :  $\frac{\omega}{N} = \cos \theta$

First harmonic	$0.5 < \frac{\omega}{N} < 1$
First and Second harmonic	$0.33 < \frac{\omega}{N} < 0.5$



# Experimental setup & parameters

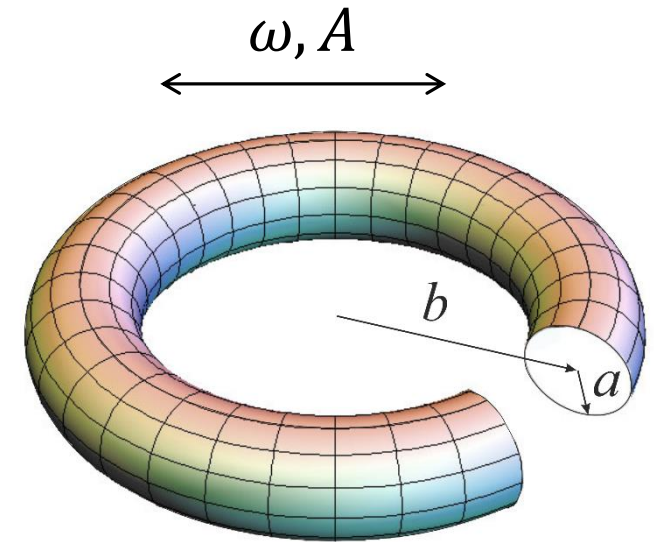


$$N = \left[ \left( -\frac{g}{\rho} \right) \left( \frac{\partial \rho}{\partial z} \right) \right]^{1/2}$$

$$Ke = \frac{A}{a}$$

$$St = \frac{\omega a^2}{\nu}$$

$$Re = \frac{2a \cdot \omega A}{\nu}$$

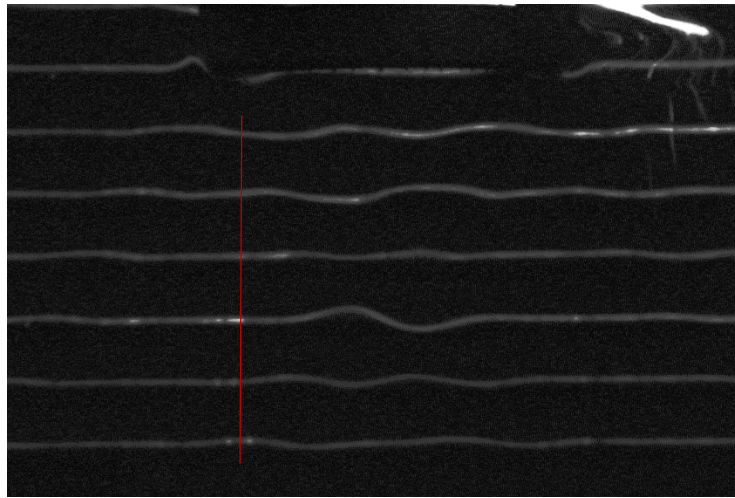


$$\varepsilon = \frac{b}{a} = 5$$

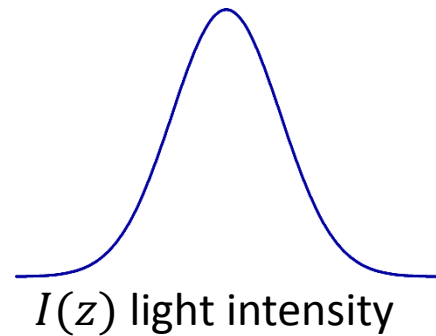
$$\frac{\omega}{N} = 0.8, 0.45$$

# Data processing

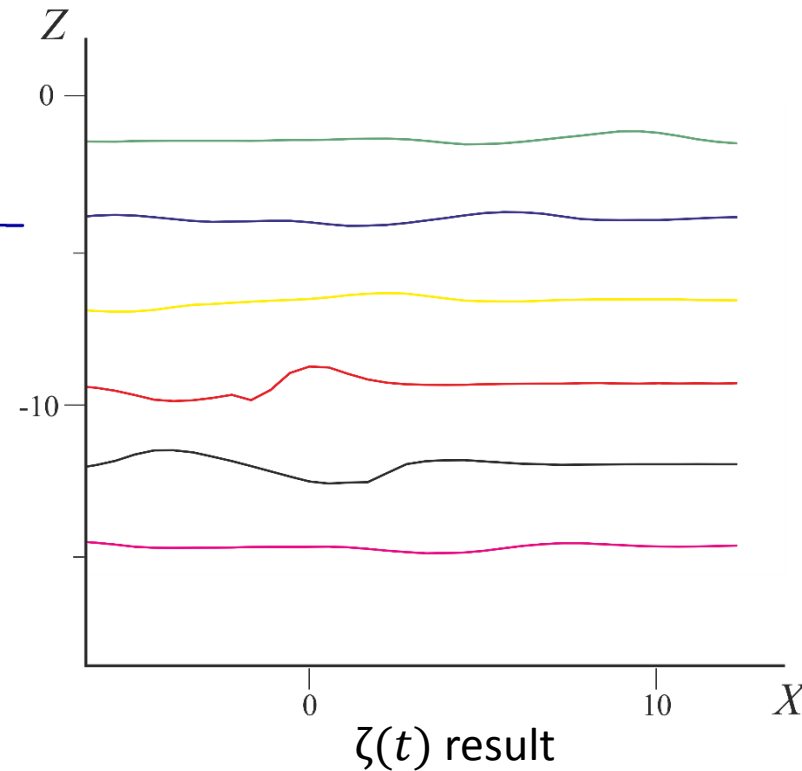
$$G(z, z', s_0) = e^{-\frac{(z-z')^2}{2s_0}} / \sqrt{2ps_0} \quad \text{Gaussian}$$



Typical image



$$C_k = \sum_{n=0}^{N-1} G_n I_{n+k}$$



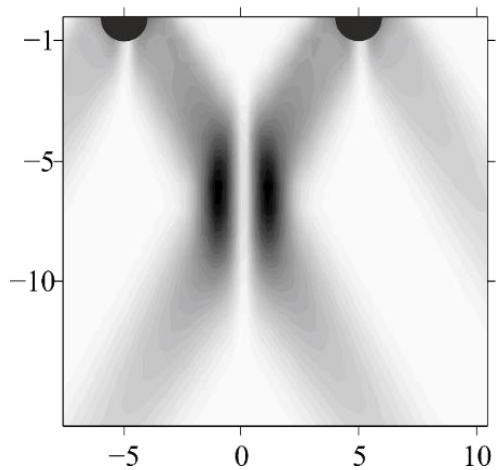
Vertical displacement  
 $\Delta\zeta(t) = \zeta(t + \delta t) - \zeta(t)$

Vertical velocity  
 $w(t) = \Delta\zeta(t)/\Delta t$

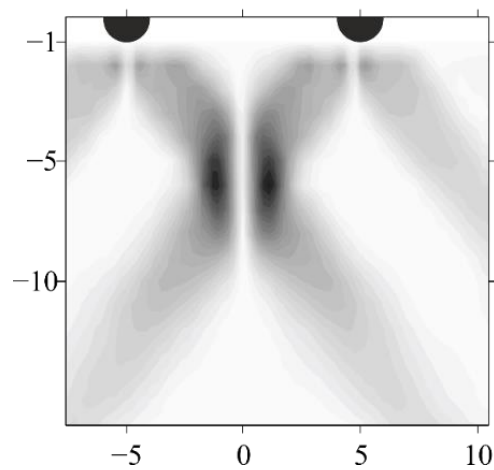
# LIF results: Vertical Velocity

$$\omega/N = 0.85$$

$$St = 222$$

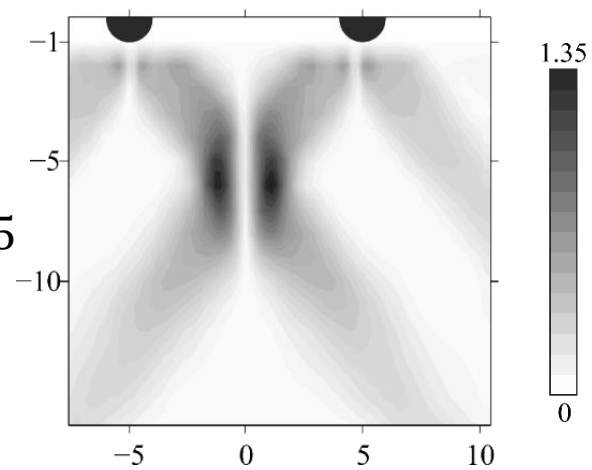


*Theory*



*Total*

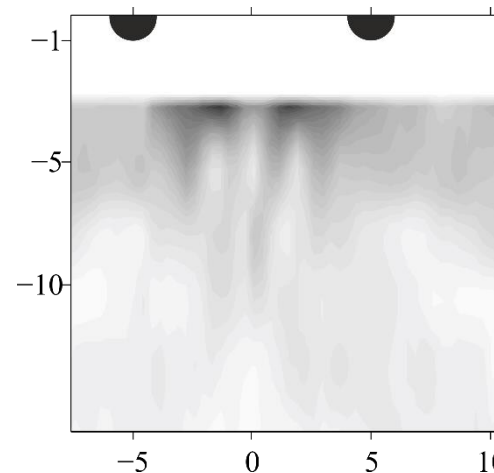
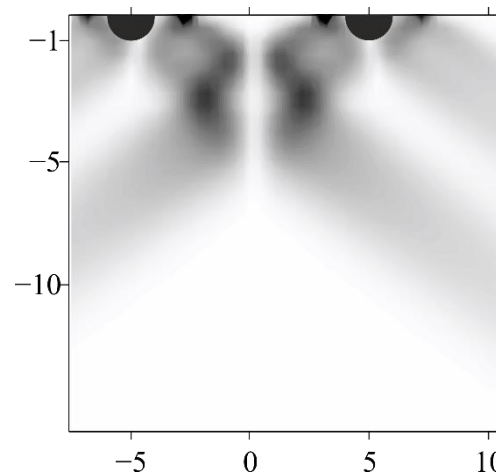
$$Ke = 0.15$$



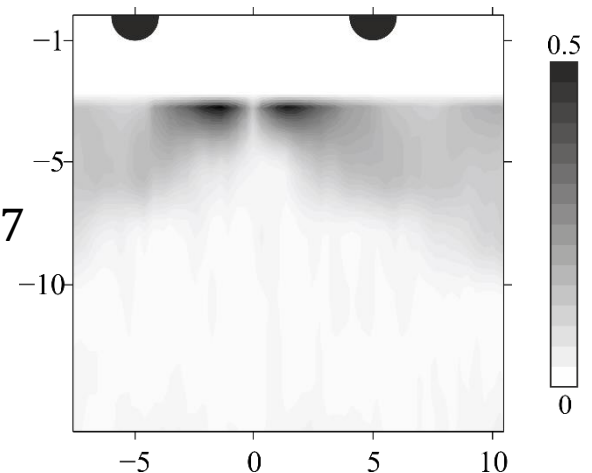
*1st Harmonic*

$$\omega/N = 0.45$$

$$St = 117$$



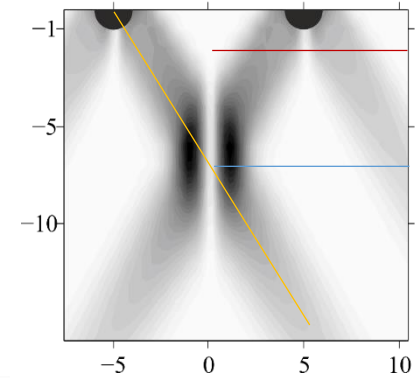
$$Ke = 0.17$$



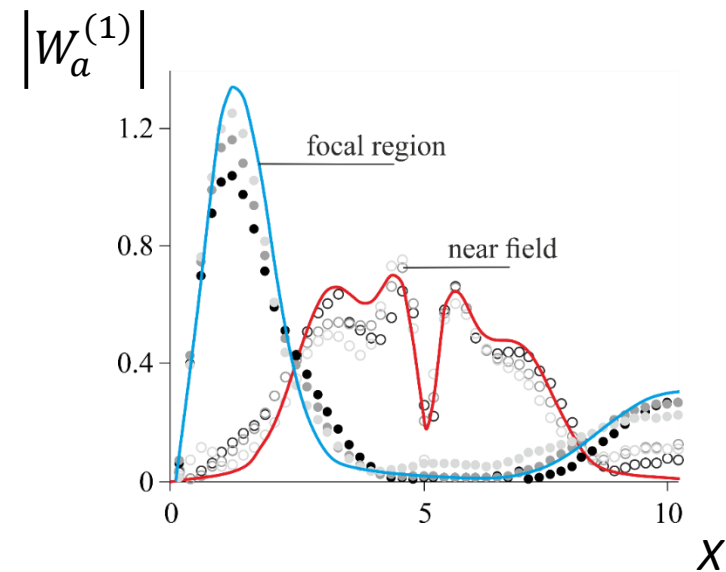
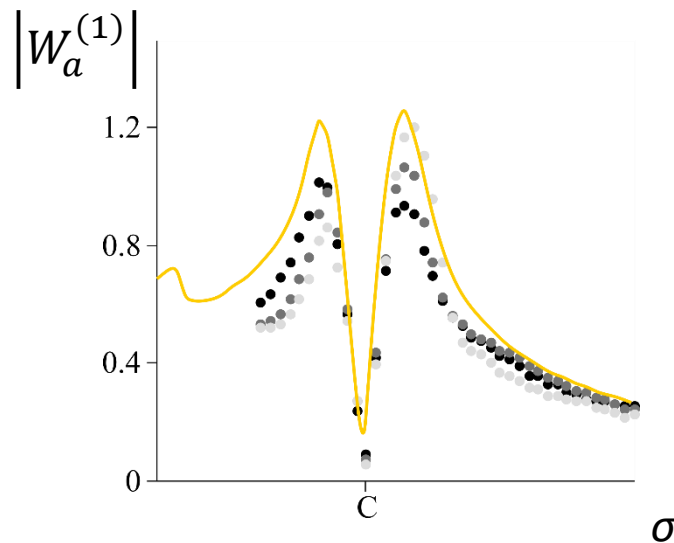
# LIF results: Vertical Velocity, comparison with linear theory

$$\omega/N = 0.85$$
$$St = 222$$

$$Ke = 0.15, 0.3, 0.52$$



Vertical  
velocity

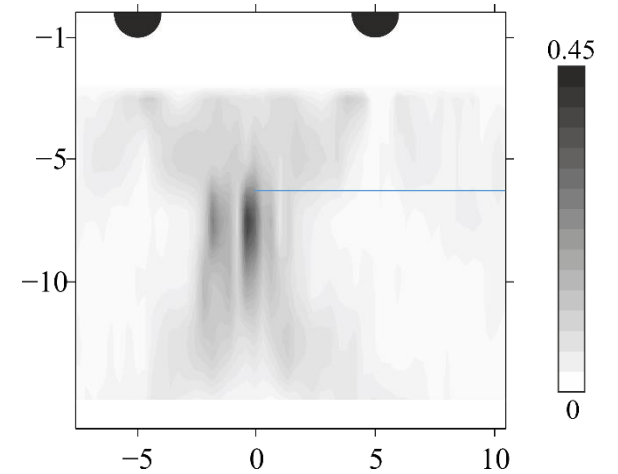
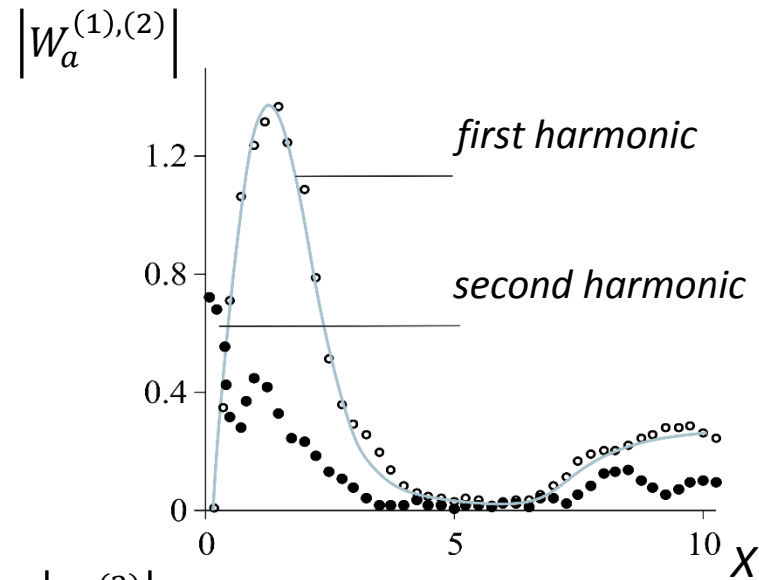


- Amplification of amplitude in focal zone
- Good comparison with linear theory

# LIF results: Second harmonics

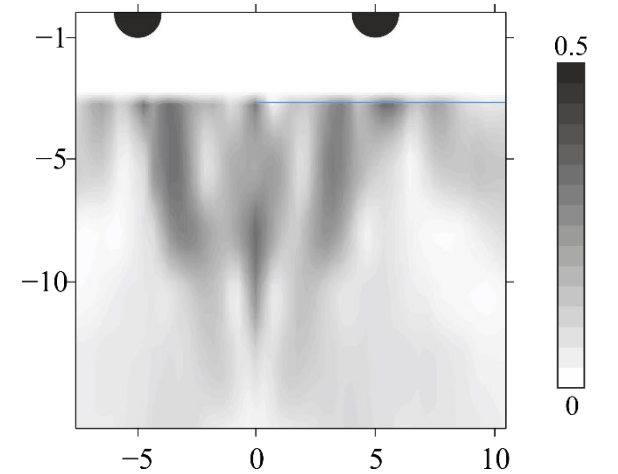
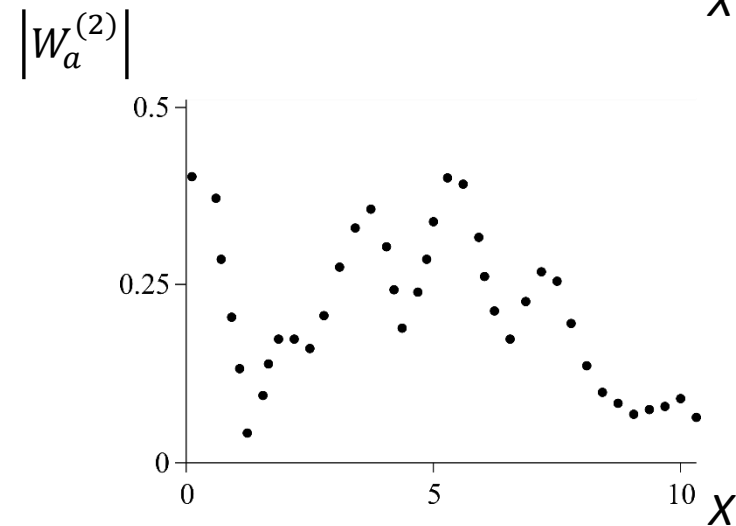
Evanescent second harmonic

$$\omega/N = 0.85$$



Propagative second harmonic

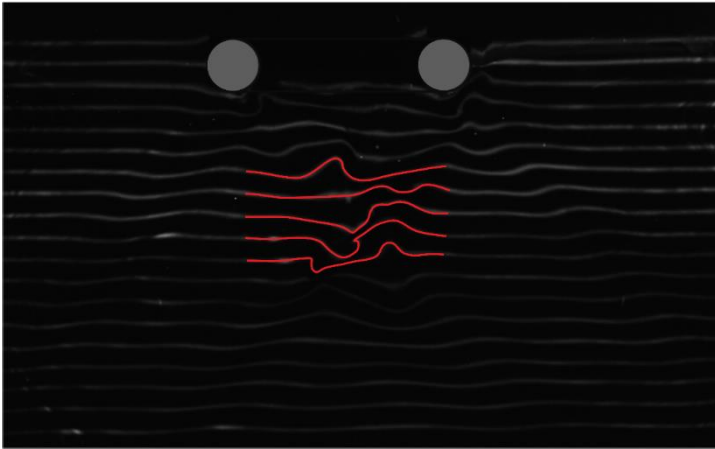
$$\omega/N = 0.45$$



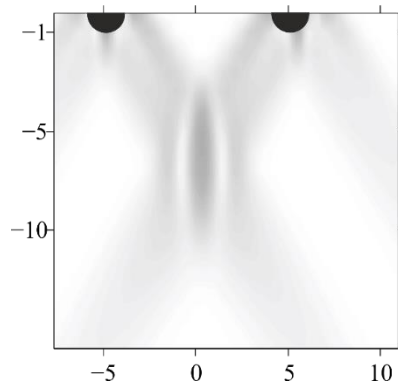


# LIF results: slopes, nonlinear effects

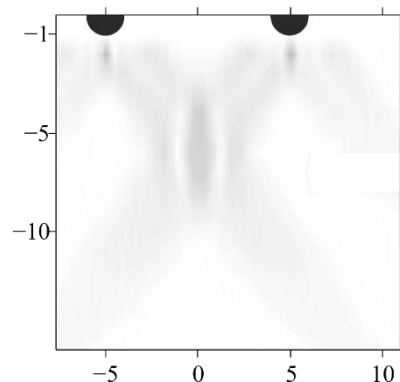
$Ke = 0.7$



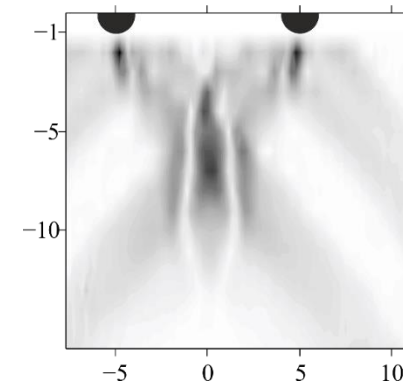
$$S_a = \overset{\text{Slope}}{\left| \arctan \left( Ke \frac{\partial W_a}{\partial X} \right) \right|}$$



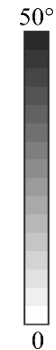
*Theory*



$Ke = 0.15$



$Ke = 0.52$



- Steep slopes at moderate  $Ke$
- Breaking of waves in the focal region

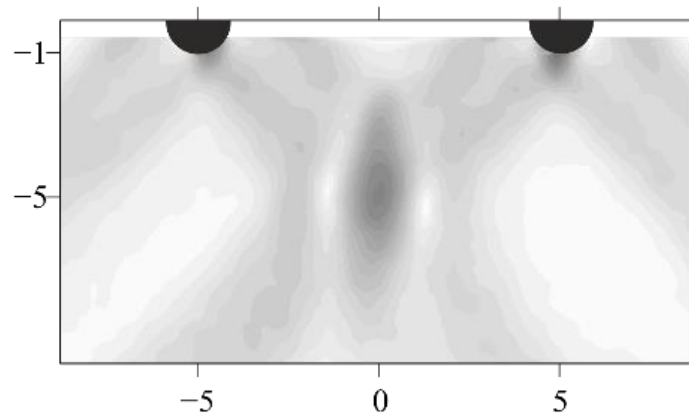
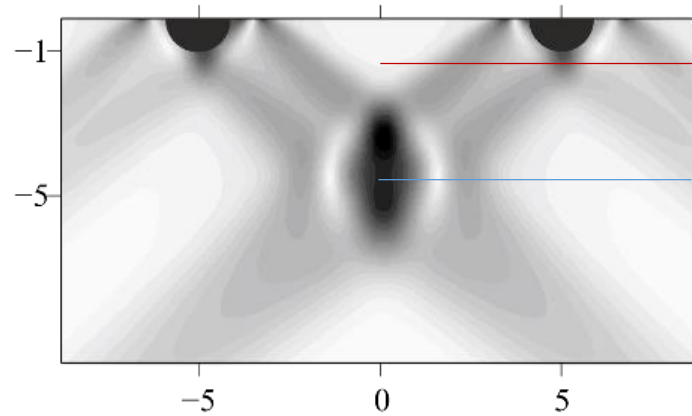
# PIV: Linear approach

Side view

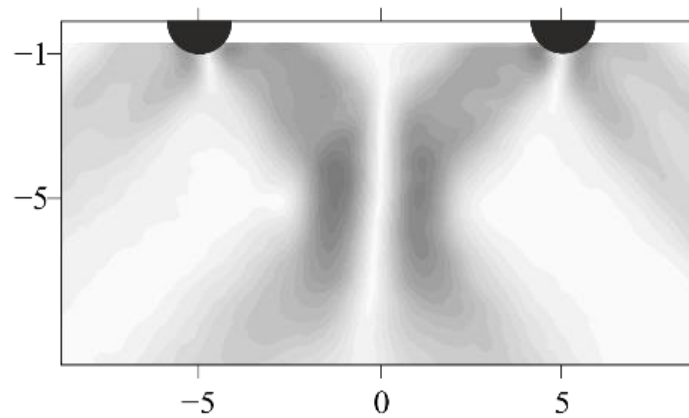
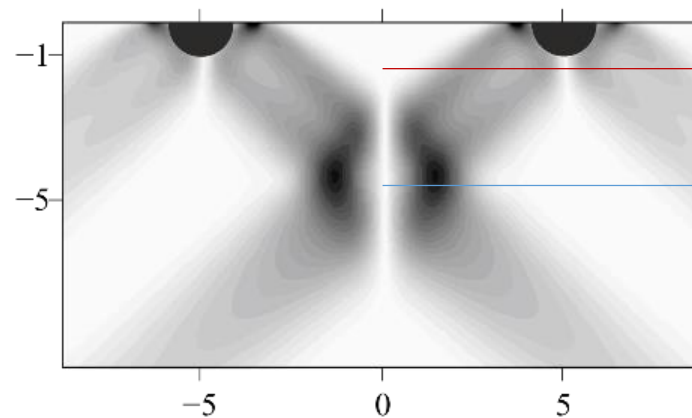
Theory

Experiment,  $Ke = 0.19$

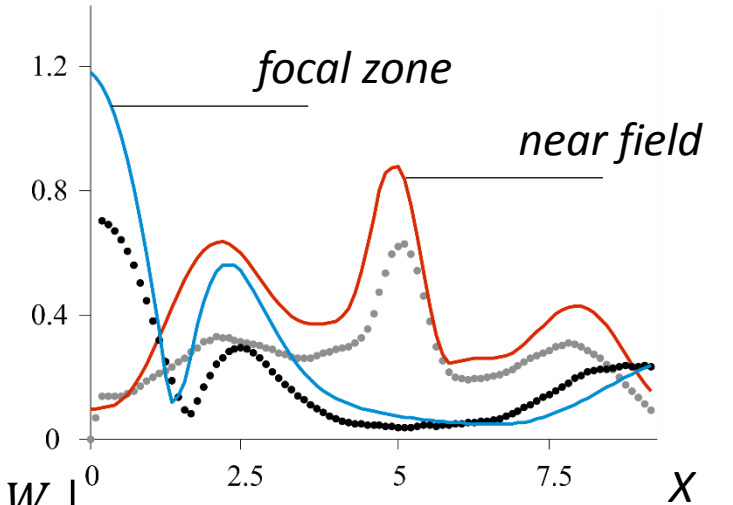
Horizontal  
velocity



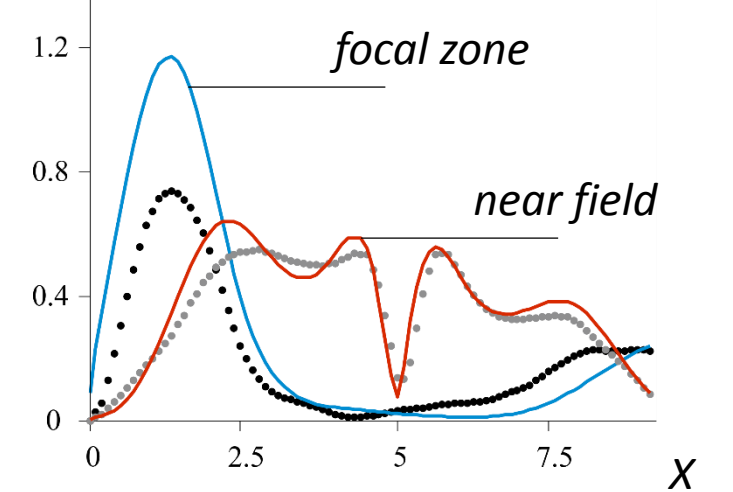
Vertical  
velocity



$|U_a|$



$|W_a|$



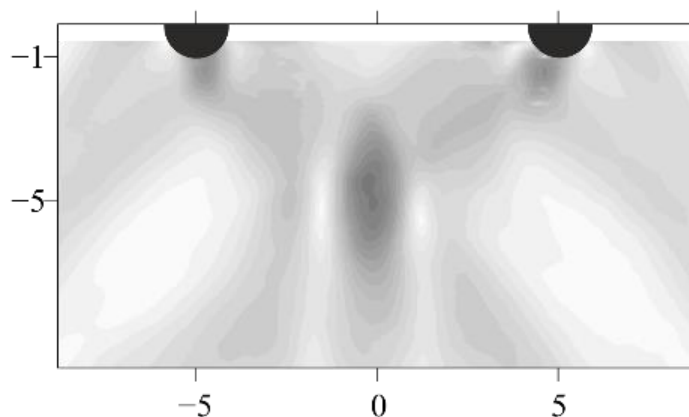
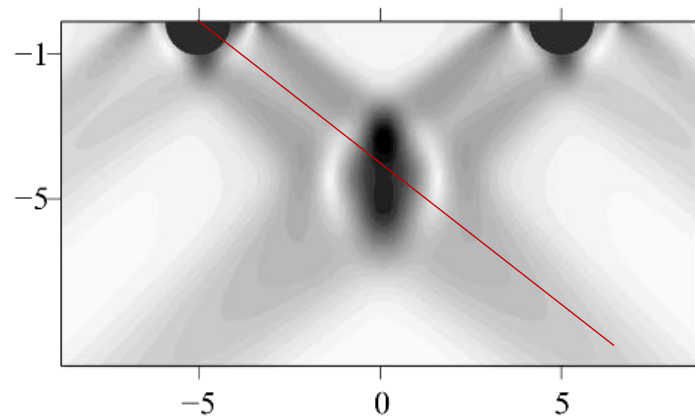
# From linear to weakly nonlinear

Side view

Theory

Experiment,  $Ke = 0.6$

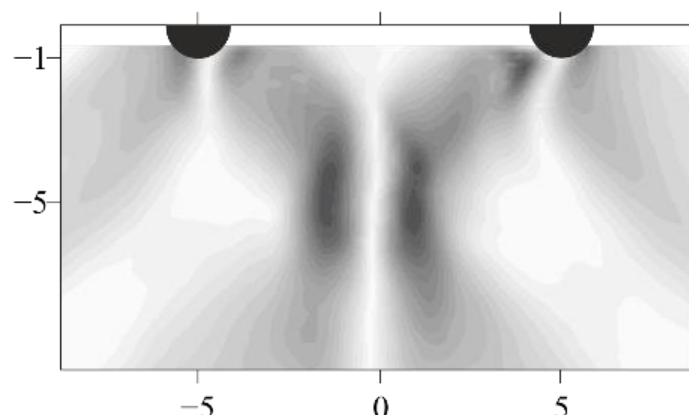
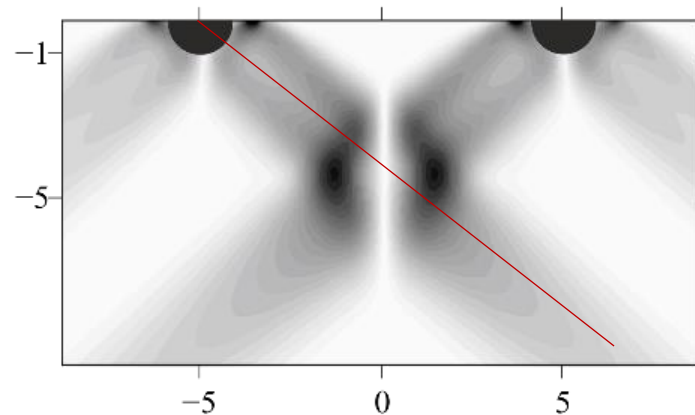
Horizontal  
velocity



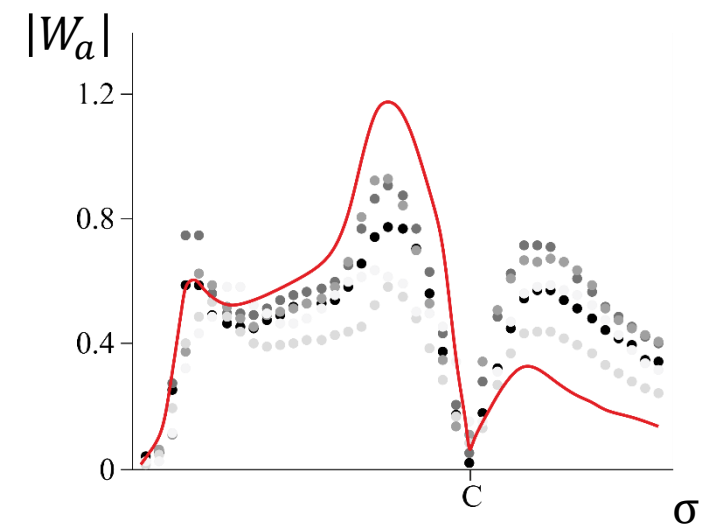
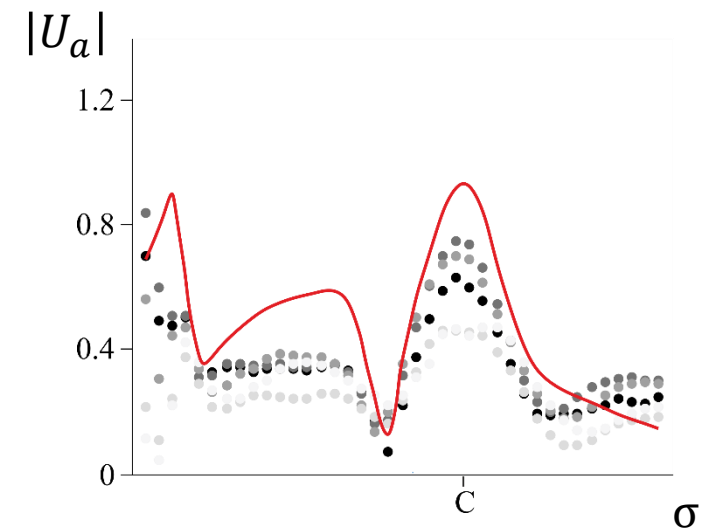
$\omega/N = 0.8$

$St = 250$

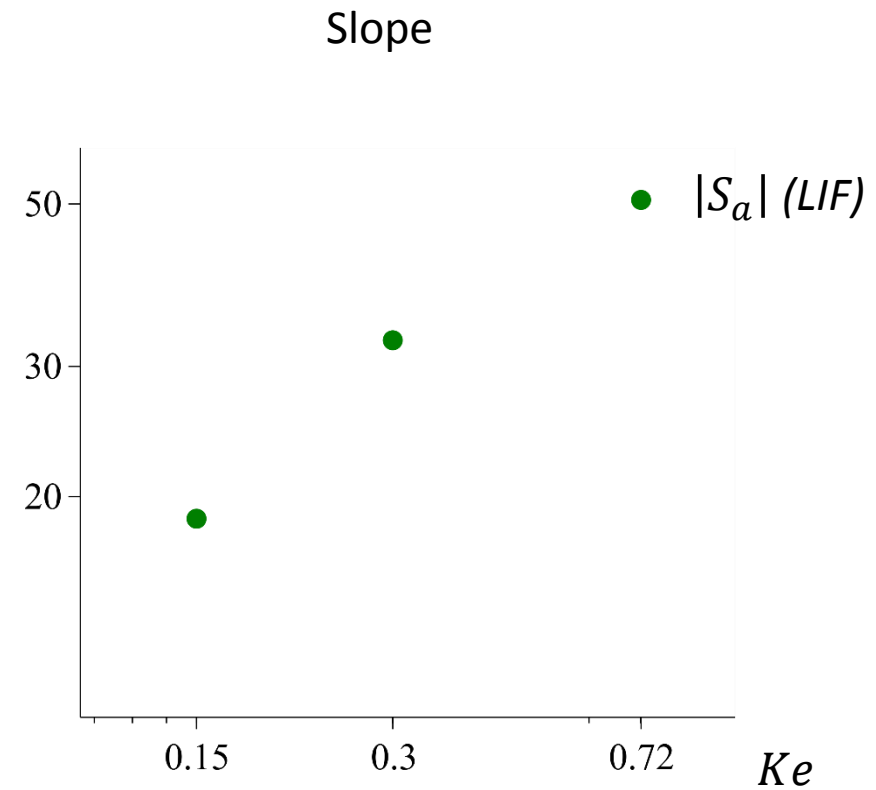
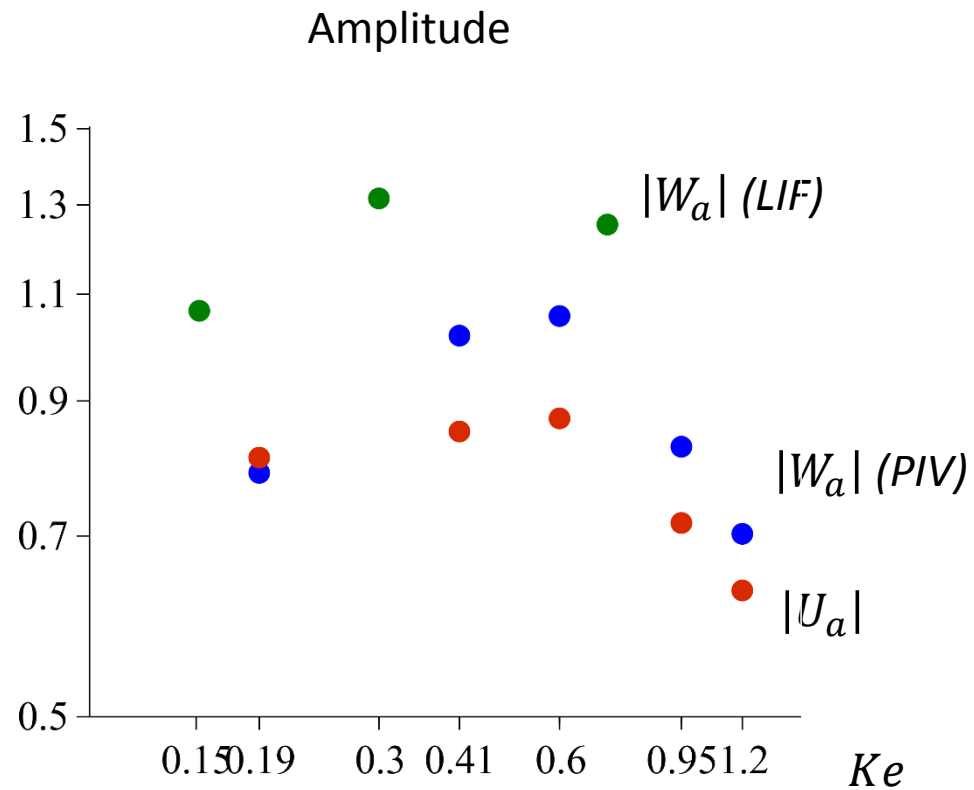
Vertical  
velocity



$Ke = 0.19, 0.41, 0.6, 0.95$

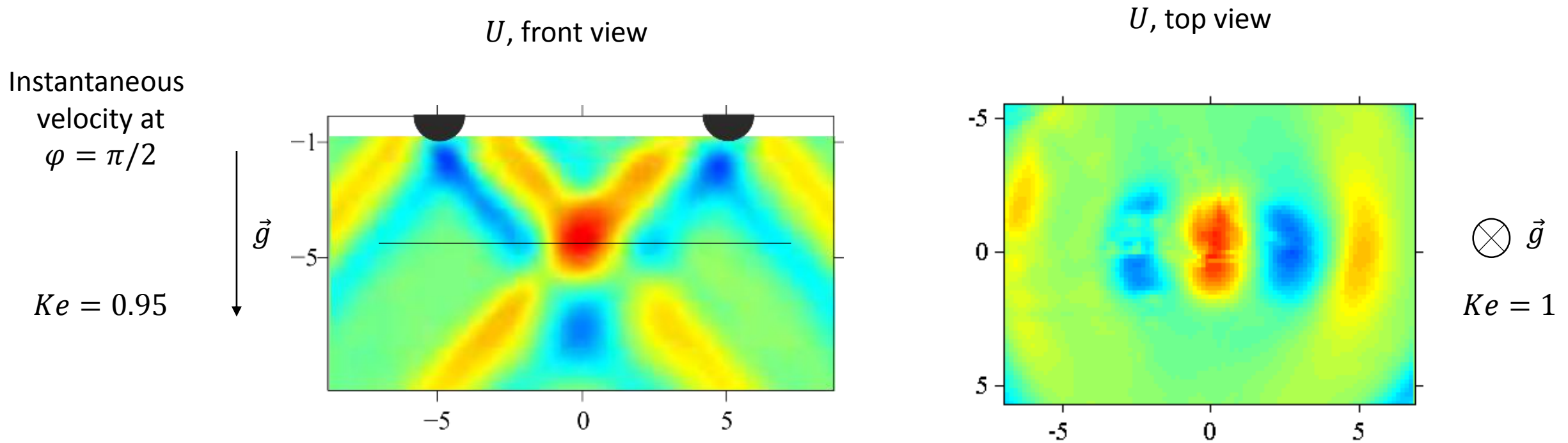


# Weakly nonlinear effects



- Moderate  $Ke$ :  
breaking before reaching the maximum amplitude;  
 $Ke_{critical} = 0.65$

# Weakly nonlinear effects



➤ Internal waves propagation from the focal region

# Conclusions

## Linear case

- Amplification of the amplitude in focal zone
- Good comparison with linear theory

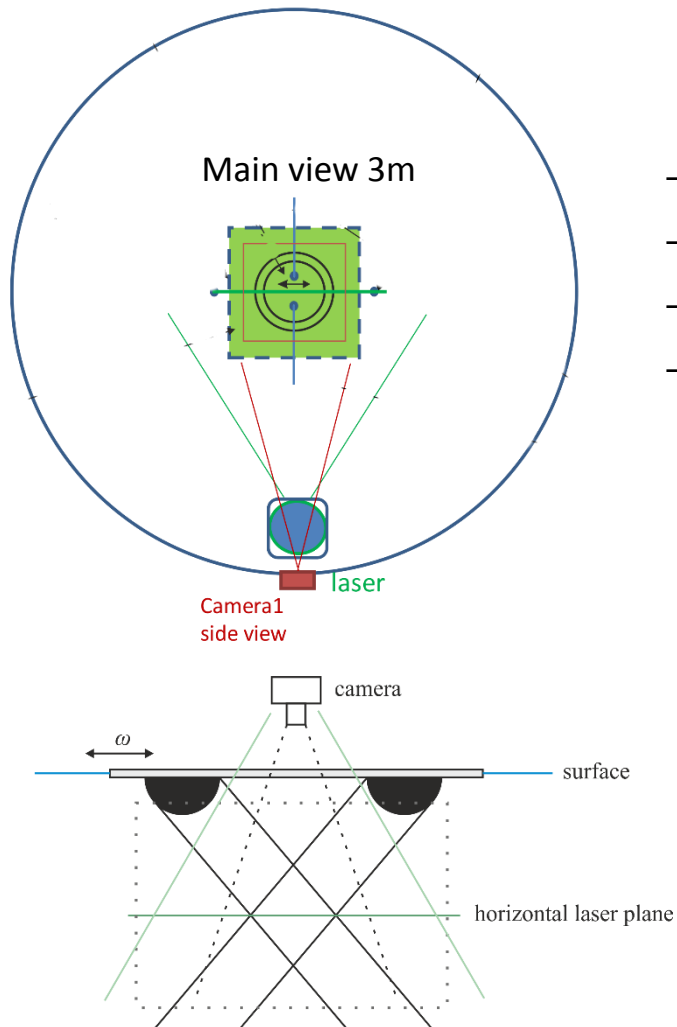
## Weakly nonlinear effects

- Presence of higher harmonics in the focal zone
- Horizontal radiation of waves from the focal zone
- Steep slopes at moderate  $Ke$

Next step: strongly nonlinear effects and turbulence

Need higher  $St$ ,  $Re \rightarrow$  larger radius of generatrix  $a$

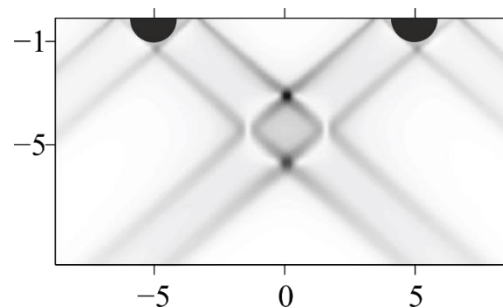
# Experimental study of wave induced turbulence on the Coriolis platform



	Small Tank	Coriolis platform
$a$	2 cm	15 cm
$b$	10 cm	75 cm
$St$	250	9900
$Re_{focal}$	150	3000

1. Internal gravity waves and higher harmonics; breaking and generation of momentum
2. Turbulence generated by
  - Internal gravity waves
  - Inertia-gravity waves
  - Inertial waves

Horizontal velocity



Vertical velocity

